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REMARKS ON THE FISSION-CAPTURE RATIO OF 25

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The capture-fission ratio $\alpha = \sigma_{\text{capture}} / \sigma_{\text{fission}}$ of 25 can be measured at thermal energies but this measurement cannot be extended to energies occurring in the fission spectrum. Therefore theoretical considerations to estimate the energy dependence of α are relevant.

The ratio α is given by

$$\alpha = \frac{\Gamma_r}{\Gamma_f}$$

where Γ_r and Γ_f are the partial widths in respect to radiation and to fission respectively. We are interested in the ratio K of the values of α at low energies to the values around 1 MeV:

$$K = \frac{(\Gamma_r)_{1 \text{ MeV}}}{(\Gamma_r)_{1 \text{ eV}}} \frac{(\Gamma_f)_{1 \text{ eV}}}{(\Gamma_f)_{1 \text{ MeV}}} \quad (1)$$

The expression for σ_f at 1 MeV is given by:

$$\sigma_f = \left\{ \sigma_0 \frac{\Gamma_f}{\Gamma_f + \Gamma_n + \Gamma_r} \right\} \quad (2)$$

σ_0 is taken as πR^2 (R nuclear radius), which defines the sticking probability. Since for 1 MeV: $R/\lambda = 2.3$, { won't be

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larger than unity. Γ_n is the neutron width, which consists of several terms: $\Gamma_n = \Gamma_{no} + \Gamma_{n1} + \Gamma_{n2} + \dots$, corresponding to the elastic reemission (Γ_{no}) and to the inelastic emissions Γ_{ni} . If $R > \lambda$, the following relation holds:¹⁾

$$\Gamma_{no} = \left\{ \sum_{\ell=0}^L (2\ell + 1) \frac{D_\ell}{\pi} \right.$$

L is the maximum ℓ which can get into the nucleus ($L = R/\lambda$) and D_ℓ is the average distance between the states which can be formed by neutrons with the angular momentum ℓ , by collision with a nucleus in a state with definite quantum numbers. Let us call Δ the distance between degenerate levels of given angular momentum, J , and assume Δ independent of J , we get $D_\ell = \frac{\Delta}{2(2\ell + 1)}$, the factor 2 coming from the spin. One then gets

$$\Gamma_{no} = \left\{ \frac{L+1}{\pi} \frac{\Delta}{2} \right.$$

We may neglect Γ_r in (2) for 1 MeV and get for Γ_f :

$$\Gamma_f = \frac{\Gamma_n}{\left\{ \frac{\sigma_0}{\sigma_f} - 1 \right.}$$

We then write: $\Gamma_n = N \Gamma_{no}$ where $N > 1$ is related to the number of levels which can be reached via inelastic scattering of 1 MeV neutrons. It is somewhat smaller than this number because Γ_{ni} is

1) See Bohr and Wheeler Phys. Rev. 56, 426 (1939) and also LA-24 (33 and 34) page 8, formula 17.

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smaller than Γ_{no} . We then get for Γ_f :

$$\Gamma_f = \left[\left\{ N / \left(\frac{\sigma_0}{\sigma_f} \right) \right\} - 1 \right] \frac{L+1}{\pi} \frac{\Delta}{2}$$

After inserting $L = R/\lambda = 2.2$ and $\sigma_0/\sigma_f = 2$ on the basis of the experimental value $\sigma_f = 1.6 \text{ barns}^1$ and $\sigma_0 = \pi R^2 = 3 \text{ barns}$, one obtains:

$$\Gamma_f = \frac{N\Delta}{2j-1} \frac{\Delta}{2}$$

Δ can be estimated in the following way: At thermal energies $\Delta/2$ is just equal to the level distance D_0 between the levels observed by McDaniel.²⁾ (The factor two comes from the fact that the neutrons excite levels with two values of J .) The decrease of the level distance from thermal energies to 1 MeV can be estimated by using a dependence $e^{-\sqrt{aE}}$ for the level distance (E is the excitation of the compound nucleus) and by adjusting the constant a so that the level distance decreases from 100 - 300 kilovolts at $E = 0$, to 2 eV at $E = 6 \text{ MeV}$. We then obtain $a = 22 (\text{MeV})^{-1}$ and a decrease of Δ by a factor of 2.5 if E is raised from 6 to 7 MeV.

In order to get a lower limit on Γ_f , we put $j = 1$, $N = 2$, $\Delta/2 = 1/3 D_0$, and $D_0 = 1 \text{ eV}$.

This gives:

$$\Gamma_f > 0.66 \text{ eV.}$$

- 1) A. O. Hanson, CH-618
 2) LA Report in preparation.

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The most plausible value for Γ_f may be obtained by putting
 $N = 2, \xi = 0.75, D_0 = 2:$

$$(\Gamma_f)_{1 \text{ MeV}} \sim 2 \text{ eV.}$$

We used Γ_f at low energies in order to estimate K which is defined in (1). $(\Gamma_f)_{\text{low}}$ is smaller or equal to the total width Γ of the levels observed by McDaniel. According to his curves one may put:

$$\Gamma \approx 0.25 \text{ eV.}$$

One obtains for the fission width at low energies:

$$\Gamma_f = \frac{\Gamma}{1+\alpha}$$

which gives 0.2 eV with a value α of 0.25. Thus the ratio K obeys the relation:

$$K \geq 2.6 (1+\alpha)$$

*With the most probable value of Γ_f , we obtain

$$K \sim 8.$$

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